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SUPPLEMENTARY MATERIAL TO
**Thermophysical properties of binary mixtures of
N,N-dimethylformamide with three cyclic ethers**

BISWAJIT SINHA^{1*}, RAJENDRA PRADHAN², SANJOY SAHA³, DHIRAJ BRAHMAN¹
and ABHIJIT SARKAR¹

¹Department of Chemistry, University of North Bengal, Darjeeling-734013, India,

²St. Joseph's College, Darjeeling-734101, India and ³Department of Chemistry,
Kalimpong College, Kalimpong-734301, India

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TABLE S-I. Densities (ρ), viscosities (η), excess molar volumes (V_m^E), excess viscosities (η^E) for the binary mixtures of DMF (1) with the three cyclic ethers (2) at 298.15, 308.15 and 318.15 K; x_1 – mole fraction of DMF

x_1	$\rho \times 10^{-3} / \text{kg m}^{-3}$	$\eta / \text{mPa s}$	$V_m^E \times 10^6 / \text{m}^3 \text{mol}^{-1}$	$\eta^E / \text{mPa s}$
DMF (1) + THF (2)				
$T = 298.15 \text{ K}$				
0	0.8807	0.463	0	0
0.0988	0.8873	0.470	-0.058	-0.019
0.1978	0.8938	0.482	-0.099	-0.034
0.2971	0.9003	0.496	-0.131	-0.049
0.3967	0.9067	0.518	-0.146	-0.058
0.4966	0.9131	0.547	-0.153	-0.062
0.5967	0.9193	0.586	-0.135	-0.057
0.6971	0.9254	0.630	-0.101	-0.050
0.7978	0.9315	0.679	-0.061	-0.039
0.8988	0.9377	0.737	-0.021	-0.022
1	0.9442	0.803	0	0
$T = 308.15 \text{ K}$				
0	0.8712	0.428	0	0
0.0988	0.8779	0.434	-0.067	-0.016
0.1978	0.8845	0.444	-0.115	-0.029
0.2971	0.8910	0.458	-0.145	-0.039
0.3967	0.8975	0.476	-0.167	-0.047
0.4966	0.9039	0.502	-0.172	-0.048
0.5967	0.9102	0.533	-0.159	-0.045

* Corresponding author. E-mail: biswachem@gmail.com

TABLE S-I. Continued

x_1	$\rho \times 10^{-3} / \text{kg m}^{-3}$	$\eta / \text{mPa s}$	$V_m^E \times 10^6 / \text{m}^3 \text{mol}^{-1}$	$\eta^E / \text{mPa s}$
DMF (1) + THF (2)				
$T = 308.15 \text{ K}$				
0.6971	0.9164	0.570	-0.130	-0.038
0.7978	0.9227	0.614	-0.103	-0.026
0.8988	0.9289	0.659	-0.059	-0.015
1	0.9350	0.709	0	0
$T = 318.15 \text{ K}$				
0	0.8614	0.390	0	0
0.0988	0.8680	0.410	-0.054	0.002
0.1978	0.8749	0.431	-0.127	0.004
0.2971	0.8817	0.454	-0.181	0.007
0.3967	0.8885	0.478	-0.225	0.010
0.4966	0.8951	0.502	-0.242	0.012
0.5967	0.9013	0.523	-0.214	0.010
0.6971	0.9073	0.545	-0.160	0.008
0.7978	0.9134	0.568	-0.108	0.006
0.8988	0.9195	0.592	-0.049	0.003
1	0.9258	0.617	0	0
DMF (1) + 1,3-DO (2)				
$T = 298.15 \text{ K}$				
0	1.0571	0.588	0	0
0.1012	1.0454	0.567	-0.053	-0.040
0.2021	1.0338	0.568	-0.096	-0.058
0.3028	1.0222	0.578	-0.121	-0.068
0.4032	1.0106	0.594	-0.127	-0.073
0.5033	0.9991	0.614	-0.120	-0.074
0.6032	0.9876	0.642	-0.095	-0.068
0.7028	0.9764	0.676	-0.073	-0.056
0.8021	0.9654	0.715	-0.046	-0.040
0.9012	0.9546	0.759	-0.017	-0.020
1	0.9442	0.803	0	0
$T = 308.15 \text{ K}$				
0	1.0459	0.513	0	0
0.1012	1.0345	0.506	-0.059	-0.024
0.2021	1.0232	0.510	-0.108	-0.038
0.3028	1.0119	0.520	-0.140	-0.046
0.4032	1.0006	0.535	-0.153	-0.049
0.5033	0.9895	0.552	-0.162	-0.052
0.6032	0.9783	0.578	-0.145	-0.046
0.7028	0.9673	0.606	-0.124	-0.038
0.8021	0.9564	0.637	-0.091	-0.028
0.9012	0.9456	0.671	-0.047	-0.016
1	0.9350	0.709	0	0

TABLE S-I. Continued

x_1	$\rho \times 10^{-3} / \text{kg m}^{-3}$	$\eta / \text{mPa s}$	$V_m^E \times 10^6 / \text{m}^3 \text{mol}^{-1}$	$\eta^E / \text{mPa s}$
DMF (1) + 1,3-DO (2)				
$T = 318.15 \text{ K}$				
0	1.0334	0.458	0	0
0.1012	1.0221	0.467	-0.040	-0.005
0.2021	1.0115	0.477	-0.114	-0.009
0.3028	1.0008	0.488	-0.164	-0.013
0.4032	0.9901	0.500	-0.196	-0.016
0.5033	0.9793	0.515	-0.204	-0.017
0.6032	0.9683	0.534	-0.178	-0.014
0.7028	0.9573	0.555	-0.132	-0.010
0.8021	0.9466	0.576	-0.091	-0.006
0.9012	0.9359	0.597	-0.030	-0.002
1	0.9258	0.617	0	0
DMF (1) + 1,4-DO (2)				
$T = 298.15 \text{ K}$				
0	1.0265	1.196	0	0
0.1181	1.0173	1.109	0.028	-0.032
0.2316	1.0082	1.043	0.059	-0.048
0.3406	0.9992	0.984	0.095	-0.060
0.4455	0.9904	0.934	0.126	-0.067
0.5465	0.9820	0.891	0.135	-0.071
0.6439	0.9739	0.859	0.131	-0.066
0.7377	0.9661	0.835	0.113	-0.056
0.8282	0.9586	0.820	0.081	-0.040
0.9156	0.9513	0.811	0.044	-0.019
1	0.9442	0.803	0	0
$T = 308.15 \text{ K}$				
0	1.0166	1.013	0	0
0.1181	1.0077	0.952	0.009	-0.019
0.2316	0.9988	0.899	0.030	-0.034
0.3406	0.9902	0.849	0.039	-0.048
0.4455	0.9817	0.807	0.052	-0.057
0.5465	0.9735	0.772	0.050	-0.061
0.6439	0.9654	0.746	0.052	-0.059
0.7377	0.9576	0.726	0.039	-0.053
0.8282	0.9499	0.714	0.030	-0.040
0.9156	0.9424	0.708	0.014	-0.023
1	0.9350	0.709	0	0
$T = 318.15 \text{ K}$				
0	1.0052	0.887	0	0
0.1181	0.9968	0.843	-0.013	-0.007
0.2316	0.9886	0.797	-0.031	-0.018
0.3406	0.9804	0.753	-0.036	-0.031

TABLE S-I. Continued

x_1	$\rho \times 10^{-3} / \text{kg m}^{-3}$	$\eta / \text{mPa s}$	$V_m^E \times 10^6 / \text{m}^3 \text{mol}^{-1}$	$\eta^E / \text{mPa s}$
DMF (1) + 1,4-DO (2)				
$T = 318.15 \text{ K}$				
0.4455	0.9724	0.713	-0.046	-0.042
0.5465	0.9644	0.680	-0.045	-0.047
0.6439	0.9564	0.653	-0.034	-0.049
0.7377	0.9486	0.636	-0.028	-0.043
0.8282	0.9408	0.624	-0.012	-0.033
0.9156	0.9332	0.618	-0.002	-0.018
1	0.9258	0.617	0	0

TABLE S-II. Redlich–Kister coefficients (a_k), standard deviations (SD) for the least squares fitting of the excess molar volumes (V_m^E), excess partial molar volumes ($\bar{V}_{m,1}^E$ and $\bar{V}_{m,2}^E$) and these ($\bar{V}_{m,1}^{0,E}$ and $\bar{V}_{m,2}^{0,E}$) at infinite dilution ($\bar{V}_{m,1}^{0,E}$ and $\bar{V}_{m,2}^{0,E}$) of each component in the studied binary mixtures at $T = (298.15, 308.15 \text{ and } 318.15) \text{ K}$; molar volumes are given in $\text{cm}^3 \text{mol}^{-1}$

Parameter	DMF (1) +		
	THF (2)	1,3-DO (2)	1,4-DO (2)
$T = 298.15 \text{ K}$			
a_0	-0.596	-0.480	0.520
a_1	0.145	0.290	0.238
a_2	0.251	0.133	-0.180
a_3	0.184	-0.077	-0.058
SD	0.002	0.002	0.003
$\bar{V}_{m,1}^E$	76.75	76.86	77.58
$\bar{V}_{m,2}^E$	81.86	69.94	86.35
$\bar{V}_{m,1}^{0,E}$	-0.674	-0.560	0.160
$\bar{V}_{m,2}^{0,E}$	-0.016	-0.134	0.520
$T = 308.15 \text{ K}$			
a_0	-0.669	-0.637	0.212
a_1	0.097	0.086	0.041
a_2	-0.040	0.068	-0.119
a_3	-0.053	-0.016	0.040
SD	0.004	0.003	0.003
$\bar{V}_{m,1}^E$	77.43	77.54	78.19
$\bar{V}_{m,2}^E$	82.11	70.33	86.84
$\bar{V}_{m,1}^{0,E}$	-0.753	-0.639	0.012
$\bar{V}_{m,2}^{0,E}$	-0.665	-0.499	0.174
$T = 318.15 \text{ K}$			
a_0	-0.933	-0.819	-0.182
a_1	0.177	0.190	0.023
a_2	0.568	0.635	0.155
a_3	-0.203	-0.205	0.048
SD	0.006	0.006	0.003
$\bar{V}_{m,1}^E$	78.62	78.79	78.86

TABLE S-II. Continued

Parameter	DMF (1) +		
	THF (2)	1,3-DO (2)	1,4-DO (2)
$T = 318.15 \text{ K}$			
$\bar{V}_{m,2}^E$	83.32	71.49	87.70
$\bar{V}_{m,2}^{0,E}$	-0.339	-0.169	-0.098
$\bar{V}_{m,2}^{0,1,E}$	-0.391	-0.199	0.044

TABLE S-III. Values of enthalpy (ΔH^*) and entropy (ΔS^*) of activation of viscous flow for the binary mixtures; x_1 – mole fraction of DMF

x_1	$\Delta H^* / \text{kJ mol}^{-1}$	$\Delta S^* / \text{J K}^{-1} \text{ mol}^{-1}$	R^2
DMF (1) + THF (2)			
0	5.884	-18.150	0.9948
0.0988	4.527	-22.725	0.9902
0.1978	3.588	-25.992	0.9089
0.2971	2.695	-29.152	0.7474
0.3967	2.406	-30.410	0.5981
0.4966	2.636	-30.051	0.6587
0.5967	3.736	-26.902	0.8361
0.6971	4.958	-23.390	0.9473
0.7978	6.273	-19.605	0.9956
0.8988	7.865	-14.926	0.9999
1	9.604	-9.790	0.9972
DMF (1) + 1,3-DO (2)			
0	8.965	-8.460	0.9981
0.1012	6.775	-15.570	0.9902
0.2021	6.041	-18.118	0.9809
0.3028	5.856	-18.963	0.9783
0.4032	5.999	-18.804	0.9849
0.5033	6.158	-18.629	0.9856
0.6032	6.494	-17.973	0.9944
0.7028	7.005	-16.778	0.9971
0.8021	7.753	-16.830	0.9992
0.9012	8.687	-12.288	1.0000
1	9.604	-9.790	0.9972
DMF (1) + 1,4-DO (2)			
0	10.970	-9.314	0.9971
0.1181	10.022	-11.775	0.9970
0.2316	9.842	-11.781	0.9977
0.3406	9.810	-11.317	0.9978
0.4455	9.929	-10.405	0.9988
0.5465	9.947	-9.876	0.9996
0.6439	10.097	-8.997	1.0000
0.7377	10.014	-8.957	1.0000
0.8282	10.030	-8.673	0.9999

TABLE S-III. Continued

x_1	$\Delta H^* / \text{kJ mol}^{-1}$	$\Delta S^* / \text{J K}^{-1} \text{mol}^{-1}$	R^2
DMF (1) + 1,4-DO (2)			
0.9156	9.956	-8.754	0.9997
1	9.604	-9.790	0.9972

TABLE S-IV. Ultrasonic speeds (u), isentropic compressibilities (κ_S) and excess isentropic compressibilities (κ_S^E) of binary mixtures of DMF (1) + the cyclic ethers (2) at 298.15 K; x_1 – mole fraction of DMF; x_1 – mole fraction of DMF

x_1	$u / \text{m s}^{-1}$	$\kappa_S \times 10^{10} / \text{Pa}^{-1}$	$\kappa_S^E \times 10^{10} / \text{Pa}^{-1}$
DMF (1) + THF (2)			
0	1277.8	6.954	0
0.0988	1313.2	6.535	-0.254
0.1978	1343.8	5.196	-0.420
0.2971	1369.6	5.921	-0.513
0.3967	1395.5	5.663	-0.581
0.4966	1418.8	5.441	-0.605
0.5967	1438.1	5.260	-0.580
0.6971	1452.1	5.125	-0.500
0.7978	1462.9	5.016	-0.387
0.8988	1463.5	4.979	-0.194
1	1464.8	4.936	0
DMF (1) + 1,3-DO (2)			
0	1338.2	5.283	0
0.1012	1352.6	5.229	-0.028
0.2021	1369.8	5.155	-0.072
0.3028	1387.8	5.079	-0.117
0.4032	1406.2	5.004	-0.159
0.5033	1424.9	4.930	-0.199
0.6032	1440.4	4.880	-0.212
0.7028	1452.3	4.856	-0.199
0.8021	1460.2	4.858	-0.158
0.9012	1462.8	4.896	-0.082
1	1464.8	4.936	0
DMF (1) + 1,4-DO (2)			
0	1343.4	5.398	0
0.1181	1368.4	5.250	-0.103
0.2316	1386.5	5.160	-0.148
0.3406	1397.5	5.124	-0.137
0.4455	1404.8	5.116	-0.099
0.5465	1408.6	5.132	-0.036
0.6439	1414.5	5.122	0.010
0.7377	1422.7	5.076	0.038
0.8282	1432.7	5.029	0.053
0.9156	1446.9	4.983	0.039
1	1464.8	4.936	0

TABLE S-V. Relative predictive capabilities of various theories and empirical relations for ultrasonic speeds of the binary mixtures at 298.15 K

DMF (1) +	MRSD ^a / %				
	FLORY	CFT	NOM	IMR	IDR
THF (2)	1.96	2.50	2.86	3.15	2.43
1,3-DO (2)	1.48	1.10	1.10	1.40	1.39
1,4-DO (2)	1.74	0.70	0.76	0.76	0.72

$$^a \text{MRSD} = 100 \left[\frac{1}{N} \sum \{ (u_{\text{exp}} - u_{\text{cal}}) / u_{\text{exp}} \}^2 \right]^{1/2}; N \text{ is number of data points}$$

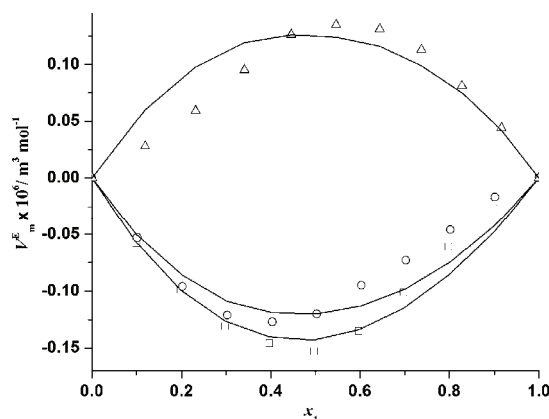


Fig. S-1. Comparison between the experimental excess molar volumes and the excess molar volumes obtained from the Prigogine–Flory–Patterson theory as a function of the mole fraction of DMF (x_1) for binary mixtures of DMF with cyclic ethers at $T = 298.15$ K. The graphical points represent the experimental excess molar volumes ($V_{m,\text{exp}}^E$): \square , THF; \circ , 1,3-DO; Δ , 1,4-DO and the smooth curves represent the $V_{m,\text{PFP}}^E$ values obtained from the Prigogine–Flory–Patterson theory.

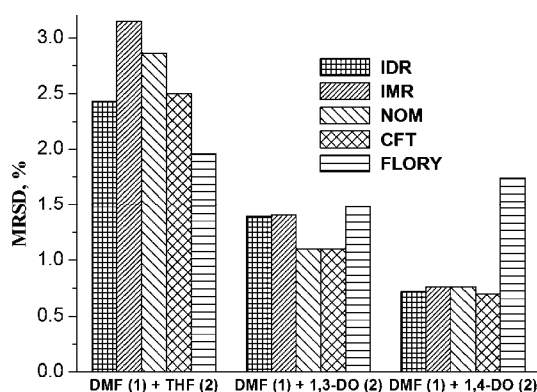


Fig. S-2. MRSD values for the theoretical prediction of the ultrasonic speeds by different theories and empirical relations for the binary mixtures of DMF + cyclic ethers at $T = 298.15$ K.