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## Effect of benzocyclobutadieno-annellation on cyclic conjugation in fluoranthene congeners

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**Abstract:** Earlier studies revealed that benzo-annellation has a peculiar effect on the intensity of cyclic conjugation in the five-membered ring of fluoranthene congeners. Now, the analogous effect of benzocyclobutadieno-annellation was examined and it was found show it is opposite to the effect of benzo-annellation: a benzocyclobutadiene fragment in angular (resp. linear) position with regard to the five-membered ring, decreases (resp. increases) the intensity of cyclic conjugation in the five-membered ring.

**Keywords:** fluoranthenes; Kekulé structure; polycyclic aromatic hydrocarbon; benzo-annellation; benzocyclobutadieno-annellation.

### INTRODUCTION

Attaching a benzene ring to a carbon–carbon bond of a polycyclic conjugated molecule can be performed in two different ways: either as an ordinary benzo-annellation or by connecting the benzene ring via two new carbon–carbon bonds, referred to as a benzocyclobutadieno-annellation (or, abbreviated, BCBD-annellation), Fig. 1.

The effect of benzo-annellation on cyclic conjugation in various polycyclic conjugated systems was much studied: in acenaphthylene and fluoranthene congeners,<sup>1–8</sup> in other non-alternant conjugated molecules,<sup>9,10</sup> and in benzenoid hydrocarbons,<sup>11–17</sup> and a general theory thereof was developed.<sup>18</sup> The analogous effect of benzocyclobutadieno-annellation has until now not been examined at all.

In previous works, particular attention was paid to the effect of benzo-annellation on the intensity of cyclic conjugation in the five-membered ring of acenaphthylene and fluoranthene congeners.<sup>1–8</sup> Within these studies, the following five generally valid regularities could be established:

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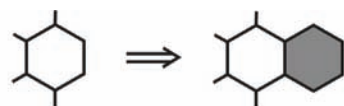
*Rule 1.* Benzo-annulation in an angular position to the five-membered ring increases the intensity of cyclic conjugation in the five-membered ring.

*Rule 2.* Benzo-annulation in a linear position to the five-membered ring decreases the intensity of cyclic conjugation in the five-membered ring.

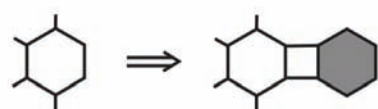
*Rule 3.* The effects specified in Rules 1 and 2 are proportional to the number of benzo-annulated rings.

*Rule 4.* The effect of an angular benzo-annulation on the intensity of cyclic conjugation in the five-membered ring is significantly stronger than the analogous effect of linear benzo-annulation.

*Rule 5.* The effect of annulation at the “male” part of fluoranthene (positions  $a_3$ ,  $a_4$  and  $l_3$ , Fig. 2) is much weaker than the effect of annulation at the “female” part (positions  $a_1$ ,  $a_2$ ,  $l_1$ , and  $l_2$ , see Fig. 2).



benzo-annulation



benzocyclobutadieno-annulation

Fig. 1. Two ways in which a benzene ring can be annulated to a polycyclic conjugated system. In this work, the effects of the benzocyclobutadieno (BCBD) annulation on the intensity of cyclic conjugation in a ring of the parent conjugated system were studied for the first time (cf. Fig. 2).

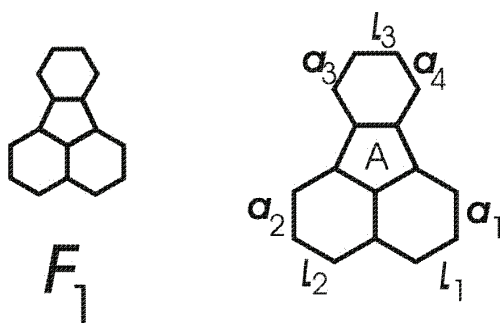


Fig. 2. Fluoranthene  $F_1$  and the sites where a benzo- or BCBD-annulation can occur. Sites marked by  $a$  and  $l$  pertain, respectively, to angular and linear annulation relative to the five-membered ring (A).

The intensity of cyclic conjugation can be assessed by means of the energy-effect ( $ef$ ) of the respective ring. The theory of the  $ef$ -method has been outlined in two reviews.<sup>19,20</sup> For additional details see an older paper,<sup>21</sup> more recent articles,<sup>16,17,22,23</sup> and elsewhere.<sup>4,11</sup> For the present considerations it is sufficient to recall that the  $ef$ -values are expressed in units of the HMO carbon-carbon resonance integral  $\beta$ . Therefore, positive  $ef$ -values indicate thermodynamic sta-

bilization caused by cyclic conjugation, and the greater is  $ef$ , the stronger is the cyclic conjugation in the considered ring.

It should be noted that in previous works,<sup>1–8</sup> instead of “angular” constellation of a five- and a six-membered ring, their “PCP” constellation (where PCP is the abbreviation of “phenyl-cyclopentadienyl”) was used. In these works,<sup>1–8</sup> RuAle 1 was referred to as the “PCP rule” or the “PCP effect”. Since in the present work, we are going to consider benzocyclobutadieno-annellation will be considered, the term “PCP” would be misleading, and, therefore, the more plausible term “angular” is used (*cf.* Fig. 1).

The regularities stated here as Rules 1–4 were first discovered by calculating the  $ef$ -values of the five-membered ring. Eventually, these regularities were confirmed by a number of other, independent, theoretical approaches.<sup>3,6,8,13</sup>

In this paper, the regularities analogous to Rules 1–4 in BCBD-derivatives of fluoranthene (**F**<sub>1</sub>) are studied. BCBD-annellation in fluoranthene may occur in the angular or in the linear mode, relative to the five-membered ring, as shown in Fig. 2.

#### NUMERICAL WORK

There exist four monobenzocyclobutadieno- (**F**<sub>2</sub>–**F**<sub>5</sub>), ten dibenzocyclobutadieno- (**F**<sub>6</sub>–**F**<sub>15</sub>), nine tribenzocyclobutadieno- (**F**<sub>16</sub>–**F**<sub>24</sub>), and three tetrabenzocyclobutadieno-fluoranthenes (**F**<sub>25</sub>–**F**<sub>27</sub>), *i.e.*, a total of 26 BCBD-annellated species. These, together with the labeling of their rings, are depicted in Figs. 3a and 3b.

The calculated energy effects of the five-membered ring (A) and of the attached benzene rings (R, S, T, U) of fluoranthene and its 26 BCBD-annellated derivatives are given in Table I. The analogous data for benzo-annellated fluoranthenes can be found in the literature.<sup>2</sup>

#### SOME REGULARITIES OBSERVED

By examining the data given in Table I, a number of regularities for the cyclic conjugation in BCBD-annellated fluoranthene-derivatives can be recognized.

The main observed regularities are the following.

**Rule 1\***. BCBD-annellation in an angular position to the five-membered ring decreases the intensity of cyclic conjugation in the five-membered ring.

**Rule 2\***. BCBD-annellation in a linear position to the five-membered ring increases the intensity of cyclic conjugation in the five-membered ring.

**Rule 3\***. The effects specified in Rules 1\* and 2\* are proportional to the number of benzo-annellated rings.

**Rule 4\***. The effect of an angular BCBD-annellation on the intensity of cyclic conjugation in the five-membered ring is significantly weaker than the analogous effect of linear BCBD-annellation.

**Rule 5\***. The same difference between “male” and “female” effects, as stated in Rule 5, exists also in the case of BCBD-annellation.

Rules 2\* and 3\* are convincingly illustrated by the following data:  $ef(\mathbf{F}_1, \mathbf{A}) = 0.0031$  (no BCBD-annellation);  $ef(\mathbf{F}_3, \mathbf{A}) = 0.0047$ ,  $ef(\mathbf{F}_5, \mathbf{A}) = 0.0036$  (one BCBD-

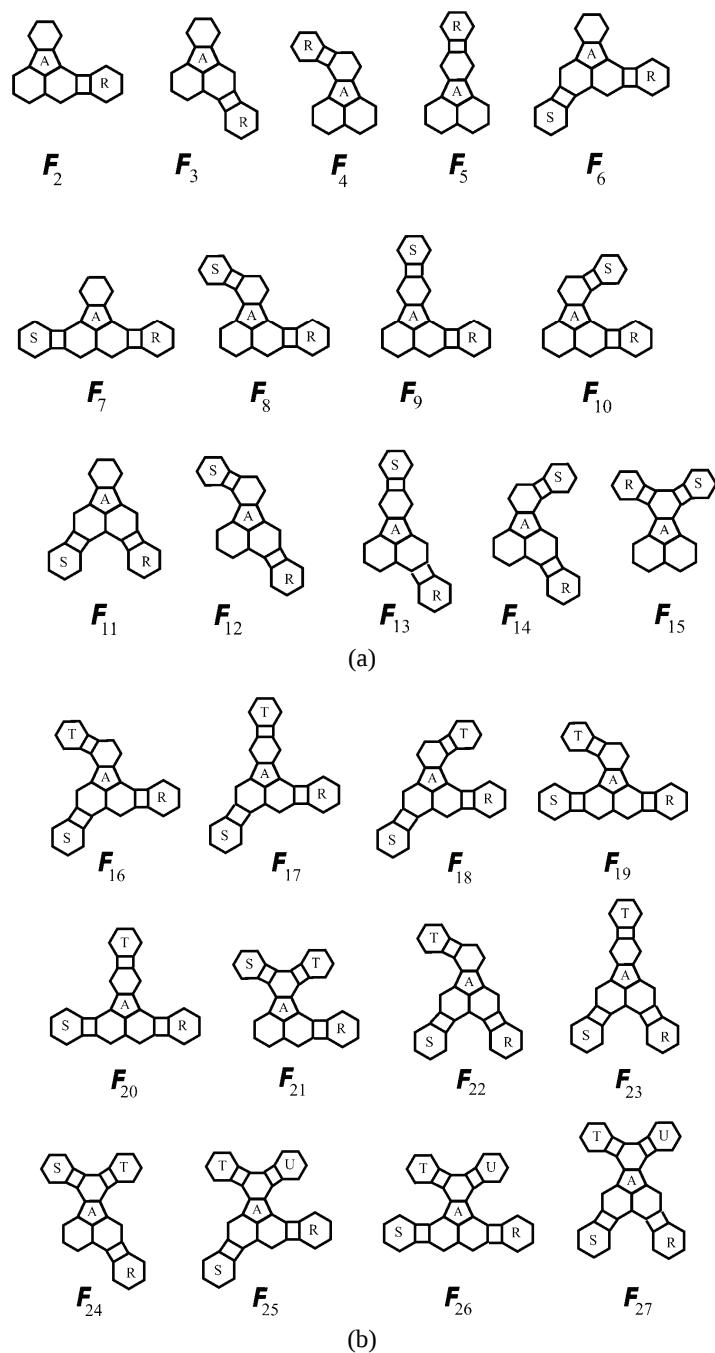


Fig. 3. a) Mono- and di-benzocyclobutadieno-annulated fluoranthenes, and b) tri- and tetra-benzocyclobutadieno-annulated fluoranthenes and the labeling of the attached benzene rings.

annellation);  $ef(\mathbf{F}_{11},A) = 0.0081$ ,  $ef(\mathbf{F}_{13},A) = 0.0060$  (two BCBD-annulations);  $ef(\mathbf{F}_{23},A) = 0.0110$  (three BCBD-annulations, maximum possible). Thus, due to Rule 2\*, the cyclic conjugation in the five-membered ring of  $\mathbf{F}_{23}$  is roughly three times greater than in fluoranthene ( $\mathbf{F}_1$ ).

TABLE I. The energy effects (in  $\beta$  units) of the five- and six-membered rings of fluoranthene and its benzocyclobutadieno-annulated congeners (depicted in Figs. 2, 3a and 3b)

| Molecule          | $ef(\mathbf{F},A)$ | $ef(\mathbf{F},R)$ | $ef(\mathbf{F},S)$ | $ef(\mathbf{F},T)$ | $ef(\mathbf{F},U)$ |
|-------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| $\mathbf{F}_1$    | 0.0031             |                    |                    |                    |                    |
| $\mathbf{F}_2$    | 0.0031             | 0.3439             |                    |                    |                    |
| $\mathbf{F}_3$    | 0.0047             | 0.5086             |                    |                    |                    |
| $\mathbf{F}_4$    | 0.0023             | 0.4459             |                    |                    |                    |
| $\mathbf{F}_5$    | 0.0036             | 0.4356             |                    |                    |                    |
| $\mathbf{F}_6$    | 0.0042             | 0.3183             | 0.5524             |                    |                    |
| $\mathbf{F}_7$    | 0.0028             | 0.3705             | 0.3705             |                    |                    |
| $\mathbf{F}_8$    | 0.0023             | 0.3433             | 0.4451             |                    |                    |
| $\mathbf{F}_9$    | 0.0036             | 0.3431             | 0.4344             |                    |                    |
| $\mathbf{F}_{10}$ | 0.0023             | 0.3438             | 0.4458             |                    |                    |
| $\mathbf{F}_{11}$ | 0.0081             | 0.4287             | 0.4287             |                    |                    |
| $\mathbf{F}_{12}$ | 0.0033             | 0.5225             | 0.4407             |                    |                    |
| $\mathbf{F}_{13}$ | 0.0060             | 0.4903             | 0.4247             |                    |                    |
| $\mathbf{F}_{14}$ | 0.0033             | 0.5245             | 0.4432             |                    |                    |
| $\mathbf{F}_{15}$ | 0.0020             | 0.3375             | 0.3375             |                    |                    |
| $\mathbf{F}_{16}$ | 0.0030             | 0.3180             | 0.5667             | 0.4434             |                    |
| $\mathbf{F}_{17}$ | 0.0052             | 0.3188             | 0.6316             | 0.4262             |                    |
| $\mathbf{F}_{18}$ | 0.0030             | 0.3184             | 0.5636             | 0.4416             |                    |
| $\mathbf{F}_{19}$ | 0.0022             | 0.3701             | 0.3705             | 0.4453             |                    |
| $\mathbf{F}_{20}$ | 0.0031             | 0.3703             | 0.3703             | 0.4343             |                    |
| $\mathbf{F}_{21}$ | 0.0020             | 0.3434             | 0.3371             | 0.3376             |                    |
| $\mathbf{F}_{22}$ | 0.0049             | 0.4463             | 0.4477             | 0.4371             |                    |
| $\mathbf{F}_{23}$ | 0.0110             | 0.4143             | 0.4143             | 0.4078             |                    |
| $\mathbf{F}_{24}$ | 0.0025             | 0.5359             | 0.3355             | 0.3370             |                    |
| $\mathbf{F}_{25}$ | 0.0023             | 0.3182             | 0.5759             | 0.3369             | 0.3358             |
| $\mathbf{F}_{26}$ | 0.0018             | 0.3702             | 0.3702             | 0.3373             | 0.3373             |
| $\mathbf{F}_{27}$ | 0.0034             | 0.4626             | 0.4626             | 0.3352             | 0.3352             |

Analogously, Rules 1\* and 3\* are illustrated by the following data:  $ef(\mathbf{F}_1,A) = 0.0031$  (no BCBD-annellation);  $ef(\mathbf{F}_2,A) = 0.0031$ ,  $ef(\mathbf{F}_4,A) = 0.0023$  (one BCBD-annellation);  $ef(\mathbf{F}_7,A) = 0.0028$ ,  $ef(\mathbf{F}_8,A) = 0.0023$ ,  $ef(\mathbf{F}_{10},A) = 0.0023$ ,  $ef(\mathbf{F}_{15},A) = 0.0020$  (two BCBD-annulations);  $ef(\mathbf{F}_{19},A) = 0.0022$ ,  $ef(\mathbf{F}_{21},A) = 0.0020$  (three BCBD-annulations);  $ef(\mathbf{F}_{26},A) = 0.018$  (four BCBD-annulations, maximum possible). Thus, due to Rule 1\*, the cyclic conjugation in the five-membered ring of  $\mathbf{F}_{26}$  is roughly two thirds that in fluoranthene ( $\mathbf{F}_1$ ).

From these examples, it can be seen that linear BCBD-annellation has a much stronger effect on cyclic conjugation in the five-membered ring than angular BCBD-annellation, as claimed by Rule 4\*.

If both linear and angular BCBD-annelations are present, then their effect is a delicate combination of the effects described by Rules 1 and 2; for details see Table I. In all studied cases, the (magnifying) effect of linear annelation dominates over the (attenuating) effect of angular annelation. A characteristic example is **F**<sub>6</sub> (one linear and one angular annelation), in which the cyclic conjugation in the five-membered ring is by some 33 % more intense than in fluoranthene itself.

There exist three pairs of isomers that differ in the position of an annelation at the sites  $a_3$  and  $a_4$  (Fig. 2). These are **F**<sub>8</sub>–**F**<sub>10</sub>, **F**<sub>12</sub>–**F**<sub>14</sub>, and **F**<sub>16</sub>–**F**<sub>18</sub>. These isomers of *cis*-like and *trans*-like types have almost identical modes of cyclic conjugation, which is just another manifestation of isoarithmeticity.<sup>2,24,25</sup> For instance, for **F**<sub>16</sub>, one has  $ef(A) = 0.0063$ ,  $ef(R) = 0.1157$ ,  $ef(S) = 0.1652$  and  $ef(T) = 0.1308$ , whereas for **F**<sub>18</sub>, they are  $ef(A) = 0.0062$ ,  $ef(R) = 0.1169$ ,  $ef(S) = 0.1653$  and  $ef(T) = 0.1321$ .

On comparing Rules 1–4 with Rules 1\*–4\*, it was immediately recognize that BCBD-annelation and benzo-annelation affect cyclic conjugation in exactly the opposite ways. In order to show the quantitative aspects of this opposite tendency, the correlation between the  $ef$ -values of the five-membered rings of benzo-annelated fluoranthenes and the  $ef$ -values in the analogous BCBD-annelated species is presented in Fig. 4.

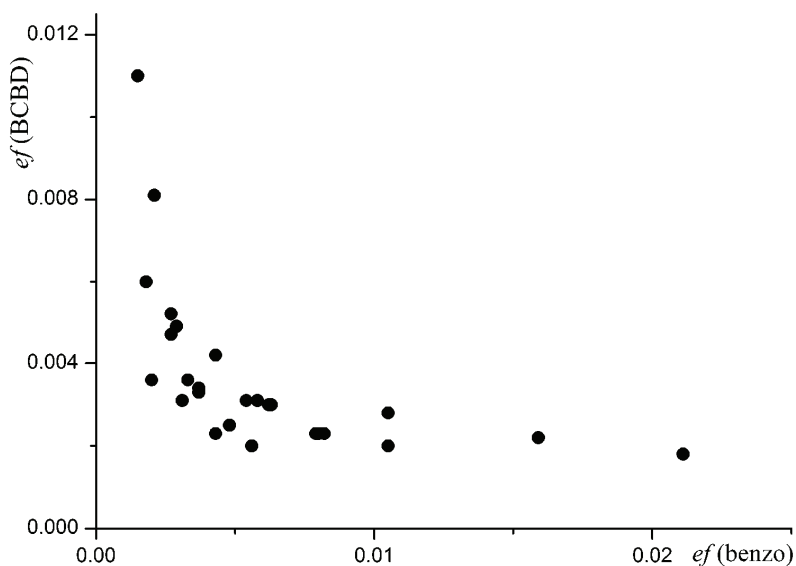


Fig. 4. The energy effects ( $ef$ ) of the five-membered rings of BCBD-annelated fluoranthenes plotted versus the corresponding  $ef$ -values of the benzo-annelated species.

Plots of the energy effects of the benzene rings in BCBD-annelated fluoranthenes versus the analogous  $ef$ -values of the benzo-annelated species are shown in Figs. 5 and 6.

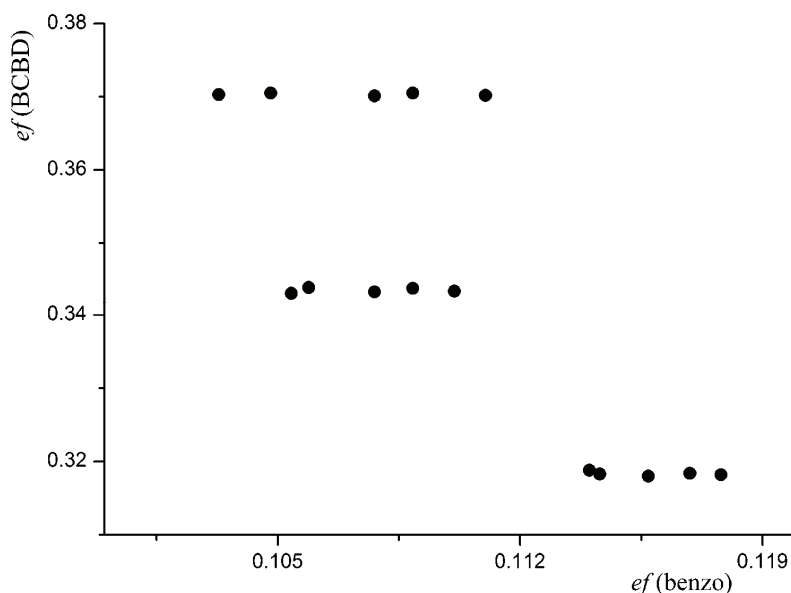


Fig. 5. The energy effects ( $ef$ ) of the benzene rings of BCBD-annelated fluoranthenes in positions  $a_1$  and/or  $a_2$  (cf. Fig. 2), plotted *versus* the corresponding  $ef$ -values of the benzo-annelated species. For details see text.

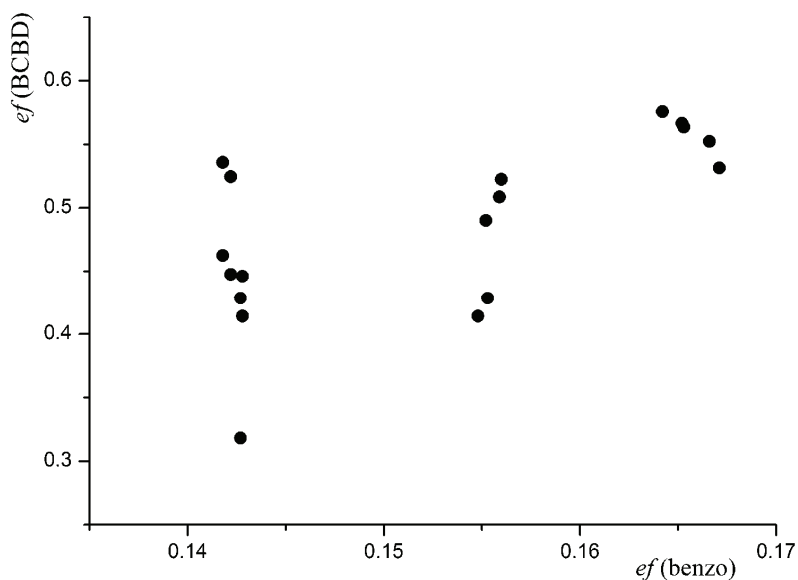


Fig. 6. The energy effects ( $ef$ ) of benzene rings of BCBD-annelated fluoranthenes in positions  $l_1$  and/or  $l_2$  (cf. Fig. 2), plotted *versus* the corresponding  $ef$ -values of the benzo-annelated species. For details see text.

Figure 5 pertains to the angularly annelated benzene rings. Only annelation in the “female” positions,  $a_1$  and/or  $a_2$ , are considered because of Rules 5 and 5\*. In harmony with Rules 1 and 1\*, it can be seen that benzo-annelation has a much stronger structure-dependency than BCBD-annelation. The data points are grouped into three clusters, depending on whether in the “female” part of the respective molecule there are two angular annelations (bottom), an angular and a linear annelation (top), or just a single angular annelation (middle).

Figure 6 pertains to the linearly annelated benzene rings. Again, in view of Rules 5 and 5\*, only annelation in the “female” positions,  $l_1$  and/or  $l_2$ , are considered. In harmony with Rules 2 and 2\*, this time BCBD-annelation has a much stronger structure-dependency than benzo-annelation. The data points are grouped into three clusters, depending on whether in the “female” part of the respective molecule there are two linear annelations (right), a linear and an angular annelation (left), or just a single linear annelation (middle).

The data in Figs. 4–6 may be viewed as illustrations of the previously established Rules 1–4, the presently established Rules 1\*–4\*, and the fundamental differences between benzo- and benzocyclobutadiene-annelations.

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#### ИЗВОД

#### УТИЦАЈ БЕНЗОЦИКЛОБУТАДИЕНСКЕ АНЕЛАЦИЈЕ НА ЦИКЛИЧНУ КОНЈУГАЦИЈУ У ЈЕДИЊЕЊИМА ФЛУОРАНТЕНСКОГ ТИПА

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Ранија истраживања показала су да бензоанелација на специфични начин утиче на интензитет цикличне конјугације у петочланом прстену једињења флуорантенског типа. У овом ради проучен је аналогни утицај бензоциклобутатиенске анелације, и показано је да је он супротан утицају бензоанелације: бензоциклобутатиенски фрагмент у ангуларном (одн. линеарном) положају у односу на петочлани прстен, умањује (одн. увећава) интензитет цикличне конјугације у петочланом прстену.

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